

## Perfect Gas Relations

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### Compressibility

The **compressibility** of a gas is defined as

$$z = \frac{P v}{R T}$$

where

- P = Pressure
- v = Specific volume
- T = Temperature
- R = Universal gas constant

For ideal gases  $z = 1$ . For real gases:

$$z = z(P^*, T^*)$$

where  $P^* = P/P_{cr}$  and  $T^* = T/T_{cr}$ .

If  $z$  for a real gas is close to one, then the gas can be modeled as an ideal gas. The condition will be satisfied when  $P^* \ll 1$  and  $T^* \gg 1$ .

### $c_P, c_v, R$ Relation

Since

$$h = u + P v$$

then

$$dh = du + d(Pv) = du + d(RT)$$

and

$$c_P dT = c_v dT + R dT$$

or

$$\boxed{c_P = c_v + R}$$

for an ideal gas. The two specific heats are weak functions of temperature.