

### Week 13

#### Lecture 1

- Mechanical Energy Reservoir (MER) is a reservoir for organized mechanical energy. MER is open to work transfer only. Its walls are adiabatic  $dQ = 0$ . It is entropy free.

$$dS = 0 \quad \text{for a MER}$$

- Entropy Change for a Control Mass (CM). Isolated system. CM interacts with TER and MER, and  $\mathcal{P}_S \geq 0$

$$dS_{CM} + dS_{TER} + dS_{MER} = d\mathcal{P}_S \geq 0$$

but  $dS_{MER} = 0$  and  $dS_{TER} = -dQ/T_{TER}$ . Therefore

$$dS_{CM} - \frac{dQ}{T_{TER}} = d\mathcal{P}_S \geq 0$$

$\mathcal{P}_S$  is not a property. It depends on the process path just like  $Q$  and  $W$ .

- SLOT for CM

$$dS_{CM} = \frac{dQ}{T_{TER}} + d\mathcal{P}_S$$

where the terms represent:

- Increase in entropy storage within CM
- Entropy inflow in CM
- Entropy production

- Integrating gives the total entropy change in CM

$$(S_2 - S_1)_{CM} = \frac{Q_{1 \rightarrow 2}}{T_{TER}} + (\mathcal{P}_S)_{1 \rightarrow 2}$$

But

$$(\mathcal{P}_S)_{1 \rightarrow 2} \geq 0$$

where  $> 0$  is the real world, and  $= 0$  when all processes within isolated system are reversible (frictionless, loss less, etc).

- $(\mathcal{P}_S)_{1 \rightarrow 2} = 0$  will be used to determine:

- Maximum efficiency of a cyclic device
- Minimum work required to run a pump
- Maximum work that can be obtained from a given system

- For any Control Mass, Reversible, Adiabatic Process

$$dS_{CM} = 0 \quad \Delta S_{CM} = S_2 - S_1 = 0$$

## Lecture 2

- Last lecture of the term.
- Last tutorial today.
- Final examination scheduled for Friday, August 6 from 9:00 to 12:00 Noon.
- Open book exam: text, lecture notes, notes from the ECE 309 Web site, and calculator. Five questions of equal value. There will be at least one heat transfer question.

- SLOT/CV

$$\dot{P}_S = \frac{\partial}{\partial t} S_{CV} - \dot{S}_{in} + \dot{S}_{out} + \sum_{i=1} \left( \frac{\dot{Q}_i}{T_i} \right)_{CV}$$

where

$$\frac{\partial}{\partial t} S_{CV} = \frac{\partial}{\partial t} \int_{CV} s \rho dV$$

and

$$\dot{S}_{in} = \int_{A_{in}} s \rho \vec{V} \cdot \vec{n} dA \quad \text{and} \quad \dot{S}_{out} = \int_{A_{out}} s \rho \vec{V} \cdot \vec{n} dA$$

- Alternative Form of SLOT/CV

$$\left( \frac{dS}{dt} \right)_{CV} = \left( s\dot{M} + \frac{\dot{Q}}{T} \right)_{in} - \left( s\dot{M} + \frac{\dot{Q}}{T} \right)_{out} + \dot{P}_S$$

- Example of a SSSF System
- Boiler and Turbine. Find  $\dot{W}_{max}$
- Continuity Equation (Conservation of Mass)

$$\dot{M}_{in} = \dot{M}_{out} = \dot{M}$$

- Define Control Volume with inflows and outflows.
- FLOT/CV

$$\left( \frac{dE}{dt} \right)_{CV} = \dot{Q} - \dot{W} + (\dot{M}h)_{in} - (\dot{M}h)_{out}$$

and

$$\left(\frac{dE}{dt}\right)_{CV} = 0$$

- SLOT/CV

$$\left(\frac{dS}{dt}\right)_{CV} = \left(\dot{M}s + \frac{\dot{Q}}{T_R}\right)_{in} - (\dot{M}s)_{out} + \dot{\mathcal{P}}_S$$

and

$$\left(\frac{dS}{dt}\right)_{CV} = 0$$

Solving for  $\dot{Q}$  we find

$$\dot{Q} = [(\dot{M}s)_{out} - (\dot{M}s)_{in} - \dot{\mathcal{P}}_S] T_R$$

Substitute into FLOT equation and solve for  $\dot{W}$

$$\dot{W} = \left\{ \dot{M}(h - T_{Rs})_{in} - \dot{M}(h - T_{Rs})_{out} \right\} - T_R \dot{\mathcal{P}}_S$$

- Definition of Specific Availability  $b$

$$b = h - T_{Rs}$$

Now

$$\dot{W} = \dot{M}(b_{in} - b_{out}) - T_R \dot{\mathcal{P}}_S \quad \text{and} \quad \dot{\mathcal{P}}_S \geq 0$$

Therefore

$$\dot{W} \leq \dot{M}(b_{in} - b_{out})$$

- Maximum Power  $\dot{W}_{max}$  occurs when  $\dot{\mathcal{P}}_S = 0$

$$\dot{W}_{max} = \dot{M}(b_{in} - b_{out})$$

- $b = h - T_{Rs}$  is also called the Exergy.

- A 2T Heat Engine
  - undergoes a cycle
  - receives  $Q_A$  from heat source at temperature  $T_A$
  - rejects heat  $Q_B$  to a heat sink at temperature  $T_B$
  - output is work  $W$
- Energy Conversion Efficiency  $\eta$

$$\eta = \frac{W(\text{work out})}{Q_A(\text{input})} < 1$$

or

$$\eta = \frac{\dot{W}(\text{power out})}{\dot{Q}_A(\text{input rate})} < 1$$

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- Carnot Efficiency
  - Steady-state
  - Zero inflow and outflow:  $M_{in} = M_{out} = 0$
  - $T_A$  and  $T_B$  are constant
- Apply FLOT/CV and SLOT/CV
- FLOT/CV

$$\left(\frac{dE}{dt}\right)_{CV} = \dot{Q}_A - \dot{Q}_B - \dot{W} + (\dot{M}h)_{in} - (\dot{M}h)_{out}$$

However

$$\left(\frac{dE}{dt}\right)_{CV} = 0, \quad (\dot{M}h)_{in} = 0, \quad (\dot{M}h)_{out} = 0$$

and

$$\dot{W} = \dot{Q}_A - \dot{Q}_B$$

- SLOT/CV

$$\left(\frac{dS}{dt}\right)_{CV} = \left(\dot{M}s + \frac{\dot{Q}_A}{T_A}\right)_{in} - \left(\dot{M}s + \frac{\dot{Q}_B}{T_B}\right)_{out} + \dot{\mathcal{P}}_S$$

However

$$\left(\frac{dS}{dt}\right)_{CV} = 0, \quad (\dot{M}s)_{in} = 0, \quad (\dot{M}s)_{out} = 0$$

Therefore

$$\frac{\dot{Q}_A}{T_A} - \frac{\dot{Q}_B}{T_B} + \dot{\mathcal{P}}_S = 0$$

and  $\dot{\mathcal{P}}_S \geq 0$ .

- Assume Reversible Heat Engine:  $\dot{\mathcal{P}}_S = 0$
- Heat Rejection to Heat Sink

$$\dot{Q}_B = \dot{Q}_A \frac{T_B}{T_A}$$

- Carnot Efficiency

$$\eta = \frac{\dot{W}}{\dot{Q}_A} = \frac{\dot{Q}_A - \dot{Q}_B}{\dot{Q}_A} = 1 - \frac{\dot{Q}_B}{\dot{Q}_A} = 1 - \frac{T_B}{T_A} < 1$$

- Carnot efficiency is upper limit on efficiency of real heat engines.
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- Example: If heat is rejected to environment at  $T_b = 285\text{ K}$ , and if the heat source is combustion gases at  $T_A = 2000\text{ K}$ , calculate the Carnot efficiency.

$$\eta = 1 - \frac{285}{2000} = 0.858$$

- Metalurgical limits the source temperature to  $T_A = 1000\text{ K}$ , now calculate the Carnot efficiency.

$$\eta = 1 - \frac{285}{1000} = 0.715$$

Most modern power plants operate at efficiencies between 40 – 50%.

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